

14.52

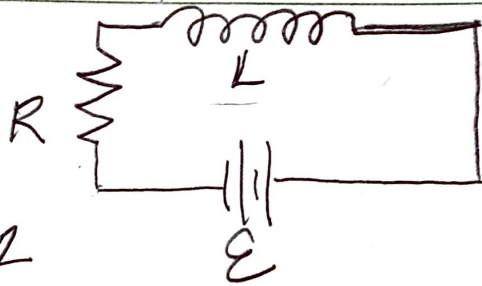


Fig 14.12

$$E = 12.0\text{V}, L = 20\text{mH} = 20 \times 10^{-3}\text{H} \text{ \& } R = 5.0\ \Omega.$$

a) Time constant for circuit. $\tau = \frac{L}{R}$

$$\tau = \frac{20 \times 10^{-3}\text{H}}{5.0\ \Omega} = \boxed{0.0040\text{s}}$$

b) Initial current = $\boxed{10\text{Amps}}$

c) Final current $I = \frac{E}{R} = \frac{12\text{V}}{5\ \Omega} = \boxed{2.4\text{A}}$

d) $I = \frac{E}{R}(1 - e^{-t/\tau})$. At 2τ ,

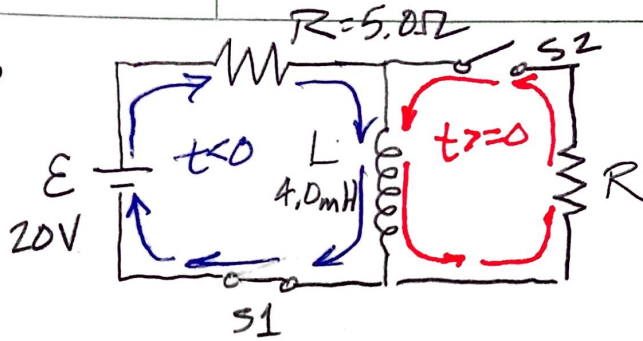
$$I = \frac{12}{5}(1 - e^{-2\tau/\tau}) = \boxed{2.08\text{A}}$$

e) At this time, when current = 2.08A

$$V_{\text{resistor}} = IR = (2.08)(5) = \boxed{10.4\text{V}}$$

$$V_{\text{inductor}} = 12 - 10.4 = \boxed{1.62\text{V}}$$

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$$\tau = \frac{L}{R} = \frac{4 \times 10^{-3} \text{ H}}{5} = 8 \times 10^{-4} \text{ s}$$

When S_1 has been closed & S_2 open, current in left side of circuit = $\frac{E}{R} = \frac{20}{5} = \boxed{4.0 \text{ A}}$

a) When switch states are changed at $t=0$, current I through L is $\frac{E}{R}$ as before, $\boxed{4.0 \text{ A}}$.

b) During discharge, $I = \frac{E}{R} e^{-t/\tau}$

$$= 4 e^{-t/8 \times 10^{-4}}$$

$$= 4 e^{-4 \times 10^{-4} / 8 \times 10^{-4}}$$

$$= \boxed{2.43 \text{ A}}$$

c) The voltages across L & R at this time?

$$V_R = IR, \text{ so } V_R = (2.43 \text{ A})(5 \Omega) = \boxed{12.1 \text{ V}}$$

Across L ? In general

$$\mathcal{E} = -L \frac{dI}{dt}, \quad \text{if } I(\text{discharging}) = \frac{E}{R} e^{-t/\tau}$$

$$\mathcal{E} = -L \frac{d}{dt} \left(\frac{E}{R} e^{-t/\tau} \right)$$

$$\frac{d}{dt} e^{-at} = -a e^{-at} \text{ (Calculus!)}$$

$$\mathcal{E} = -L \left(-\frac{1}{\tau} \right) \left(\frac{E}{R} e^{-t/\tau} \right)$$

$$\tau = \frac{L}{R}, \text{ so } \mathcal{E} = L \left(\frac{R}{L} \right) \left(\frac{E}{R} \right) e^{-t/\tau} = \boxed{E e^{-t/\tau}}$$

$$\mathcal{E} = 20 e^{-4 \times 10^{-4} / 8 \times 10^{-4}} = \boxed{12.1 \text{ V}}$$