

10.49

RC time constant τ is based on
 $C = 0.500 \mu\text{F}$ & some R value.

Need a time constant from $t = 2.00 \text{ s}$ to 15.00 s

For $t = 2.00 \text{ s} = \tau = RC$

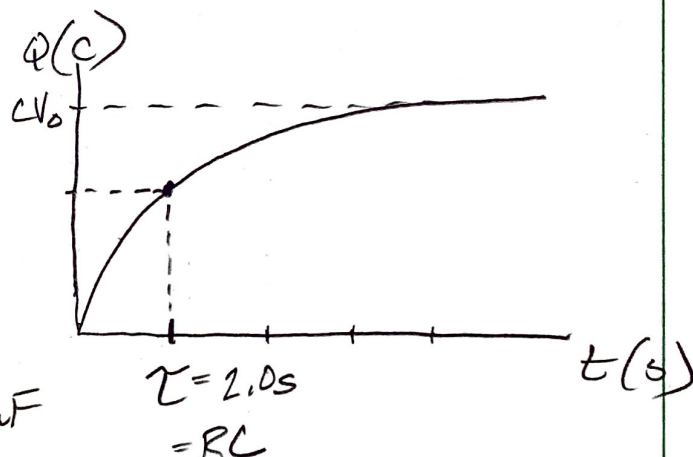
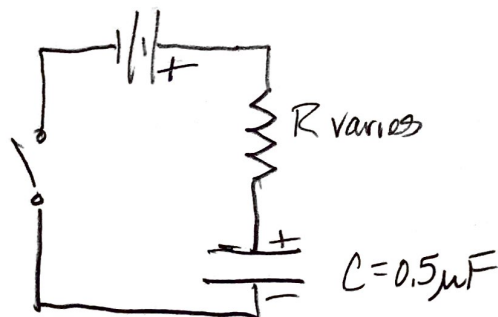
$$2.00 \text{ s} = R(0.5 \times 10^{-6})$$

$$R = \frac{2.00 \text{ s}}{0.5 \times 10^{-6}} = \boxed{4.0 \times 10^6 \Omega} = 4.0 \text{ M}\Omega$$

For $t = 15.00 \text{ s}$
 $15.0 \text{ s} = R(0.5 \times 10^{-6})$

$$R = \frac{15}{0.5 \times 10^{-6}} = \boxed{3.0 \times 10^7 \Omega} = 30 \text{ M}\Omega$$

RC Circuit



One time constant $\tau = RC$ is the amount
of time it takes for $Q = 0.632 Q_{\text{max}}$.
= 63.2% of full charge

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Paramotor fires 72x/minute $\times \frac{1 \text{ min}}{60 \text{ s}} = 1.2 \text{ times/sec}$ $\rightarrow 0.833 \text{ sec/Firing.}$ Each time it fires a $25.0 \times 10^{-9} \text{ F}$ capacitor is charged to 0.632 of its Voltage ($= 1 \tau$)

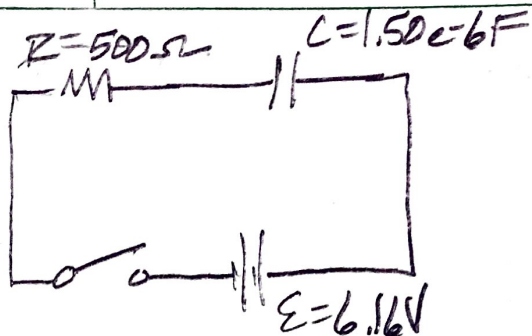
Find R.

$$\text{So } \tau = 0.833 \text{ s} = RC$$

$$0.833 \text{ s} = (R)(25 \times 10^{-9} \text{ F})$$

$$R = \frac{0.833 \text{ s}}{2.5 \times 10^{-9}} = \boxed{3.33 \times 10^8 \Omega}$$

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- a) Initial current happens when there is no ΔV across the plates of the capacitor yet.

$$I_0 = \frac{\varepsilon}{R} = \frac{6.16\text{V}}{500\Omega} = \boxed{0.123\text{A}}$$

- b) The time constant $\tau = RC$
 $= (500\Omega)(1.5 \times 10^{-6}\text{F})$
 $= \boxed{7.5 \times 10^{-4}\text{s}}$

- c) Current after one time constant (when $\tau = RC$)

$$I = \frac{V_0}{R} (e^{-t/\tau})$$

$$= \frac{6.16}{500} (e^{-1}) = \boxed{4.53 \times 10^{-3}\text{A}}$$

- d) Voltage on capacitor after one τ ?
- $$V = \frac{Q}{C}, \text{ so } V = \frac{Q}{C} = \frac{Q_0(1 - e^{-1})}{C}$$
- $$= \frac{6.16}{1} (1 - \frac{1}{e})$$
- $$= \boxed{3.89\text{V}}$$